



Universität Hamburg

DER FORSCHUNG | DER LEHRE | DER BILDUNG

MIN Faculty  
Department of Informatics



# Introduction to Robotics

## Principles of Walking

**Marc Bestmann**

bestmann@informatik.uni-hamburg.de



University of Hamburg  
Faculty of Mathematics, Informatics and Natural Sciences  
Department of Informatics

**Technical Aspects of Multimodal Systems**

May 21, 2021





Introduction

Spatial Description and Transformations

Forward Kinematics

Robot Description

Inverse Kinematics for Manipulators

Instantaneous Kinematics

Trajectory Generation 1

Trajectory Generation 2

Principles of Walking

- Introduction

- ZMP

- Linear Inverted Pendulum

- Stabilization

- Full Body Motion

Dynamics





# Outline (cont.)

Principles of Walking

Introduction to Robotics

Robot Control

Path Planning

Task/Manipulation Planning

Telerobotics

Architectures of Sensor-based Intelligent Systems

Summary

Conclusion and Outlook





- ▶ Enabling locomotion in difficult terrain
- ▶ Legs can be used for other things
- ▶ Necessary to integrate robots in a human environment



26



27

---

<sup>26</sup> [http://1.bp.blogspot.com/-MhFvPPR5V4/UmifTu4r\\_OI/AAAAAAAAAFtI/FvJqeWu9Ahc/s1600/13-pictures-of-crazy-goats-on-cliff.jpg](http://1.bp.blogspot.com/-MhFvPPR5V4/UmifTu4r_OI/AAAAAAAAAFtI/FvJqeWu9Ahc/s1600/13-pictures-of-crazy-goats-on-cliff.jpg)

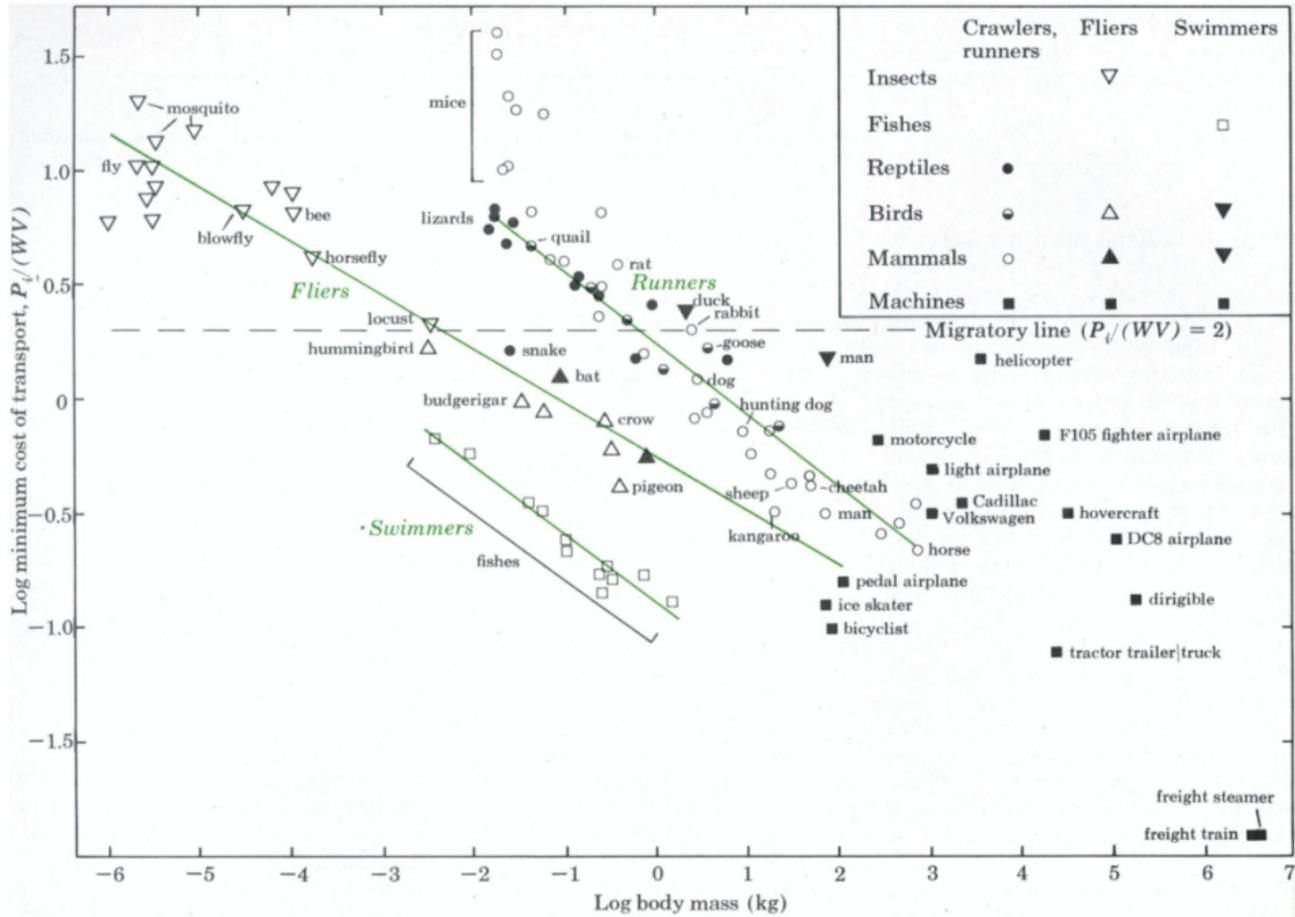
<sup>27</sup> <https://www.allposters.com>

- ▶ Stability (and safety)
- ▶ Complex control
- ▶ Hardware costs
- ▶ Energy consumption



28

wiki How to Recognize the Signs of Intoxication



29 Tucker, Vance A. "The energetic cost of moving about: walking and running are extremely inefficient forms of locomotion. Much greater efficiency is achieved by birds, fish—and bicyclists." American Scientist 63.4 (1975): 413-419.



- ▶ Static - Dynamic
- ▶ Passiv - Active
- ▶ 2,4,6,8,... legged
- ▶ Open loop - closed loop
- ▶ This lecture: active bipedal walking, no running



30



31

<sup>30</sup> <https://3c1703fe8d.site.internapcdn.net/newman/gfx/news/hires/2017/1-sixleggedrob.jpg>

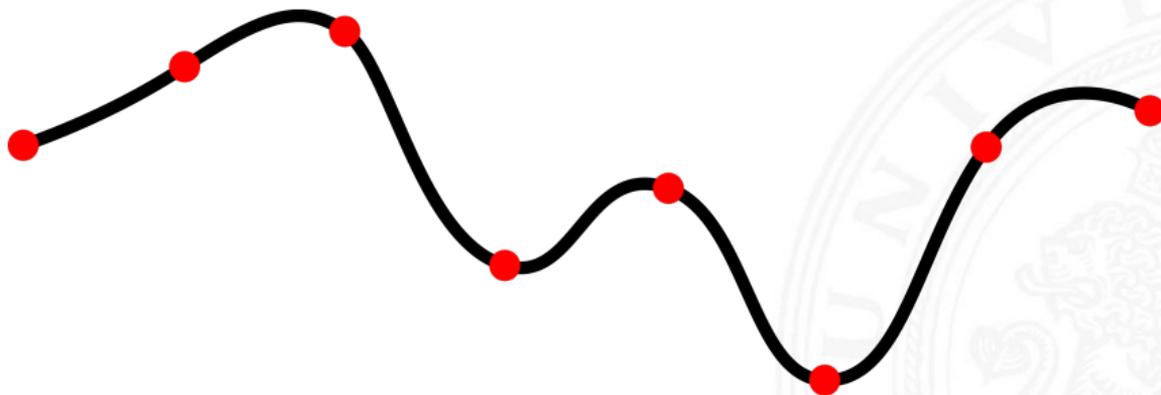
<sup>31</sup> <https://asl.ethz.ch/research/legged-robots.html>

Video





- ▶ Control Theory
- ▶ Neural Networks
- ▶ Central Pattern Generators
- ▶ Evolutional Computing
- ▶ Expert Solution



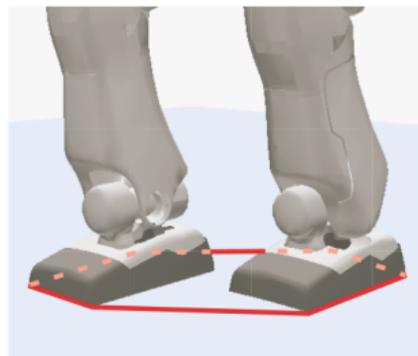


- ▶ Support leg/foot
- ▶ Flying leg/foot
- ▶ Torso / trunk
- ▶ Step / double step
- ▶ Sagittal / lateral

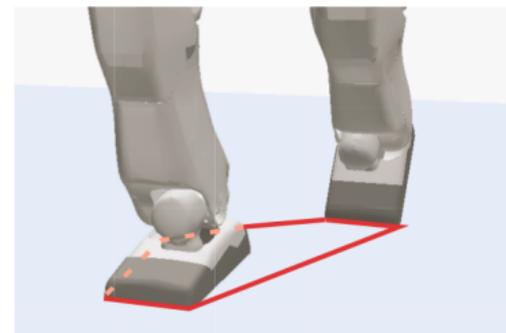
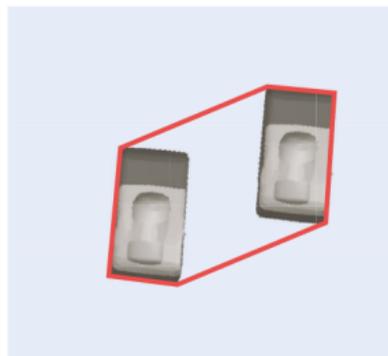




- ▶ Convex hull of all ground contact points



(a) Full contact of both feet

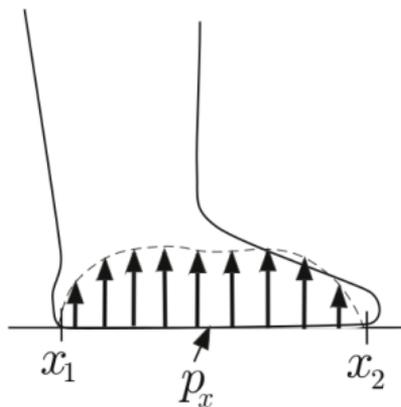


(b) Partial contact

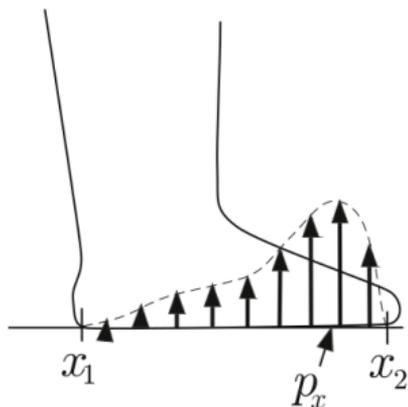
33



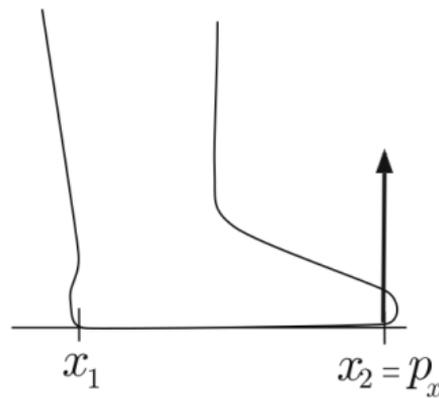
- ▶ Center of ground reaction forces
- ▶ Those can also be horizontal
- ▶ Moment becomes zero
- ▶ Equals the zero moment point (ZMP)



(a) Almost flat



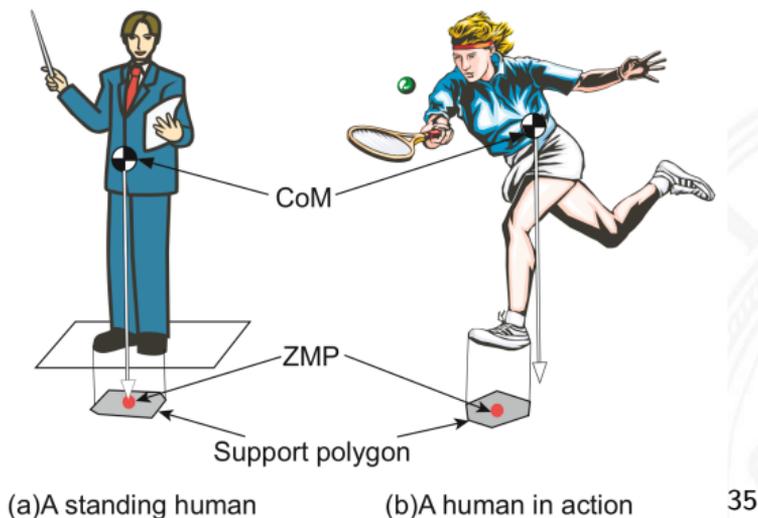
(b) Biased distribution



(c) Concentrate at tiptoe

# Zero Moment Point (ZMP)

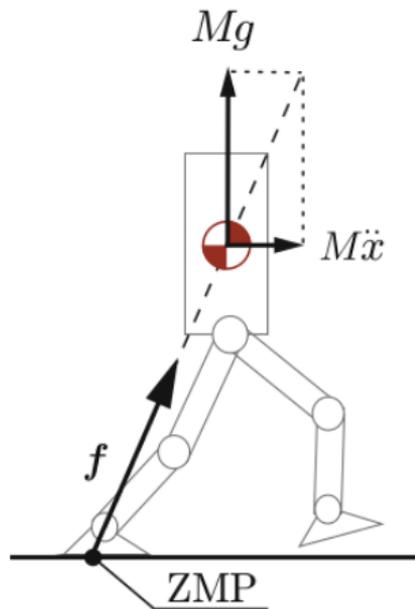
- ▶ When standing, projection of CoM coincides with ZMP
- ▶ When dynamic, CoM outside of support polygon
- ▶ ZMP is always inside support polygon



35



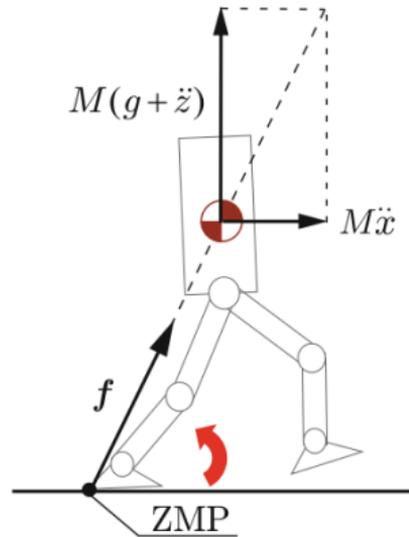
- ▶ Forces of the robot define position of ZMP
- ▶ Can it get outside of the support polygon?



36



- ▶ No! The ZMP is always in the support polygon
- ▶ If it is on an edge, the robot rotates



37

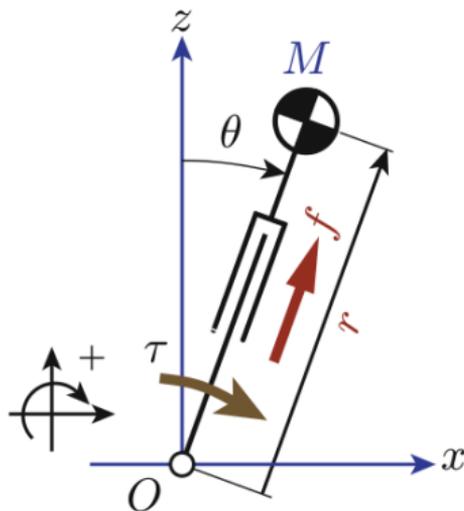
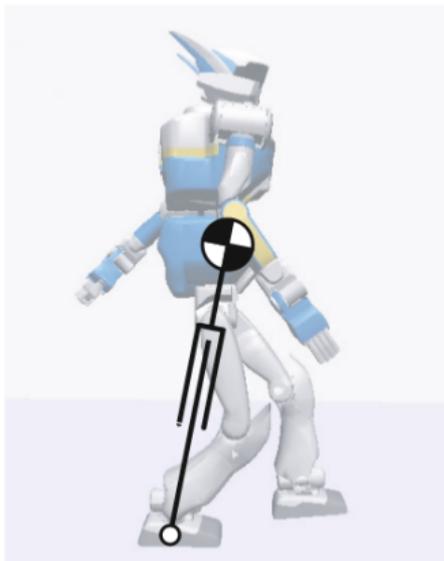


- ▶ Sole slips on ground
- ▶ Other parts of the robot are in contact with environment
- ▶ Ground is not perfectly level



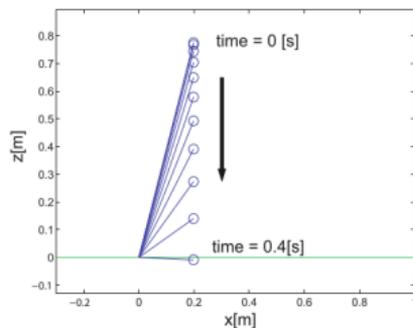
# Linear Inverted Pendulum

- ▶ Simplest model for walking robot or human
- ▶ Point mass at end of massless telescopic leg
- ▶  $f$ : kick force,  $\tau$ : torque

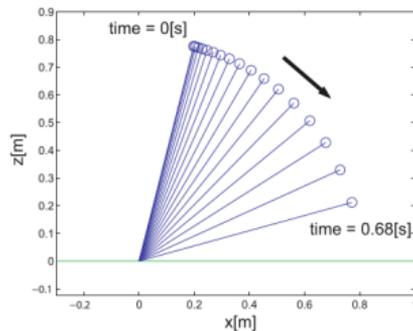


38

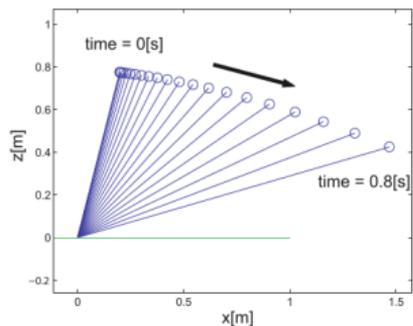
# Inverted Pendulum



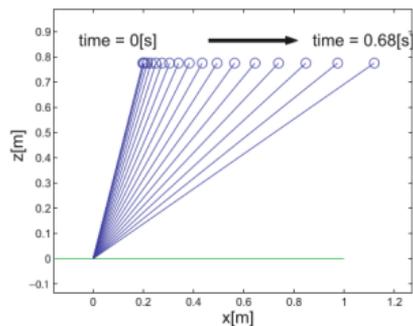
(a)  $f = 0$  : Free fall of CoM



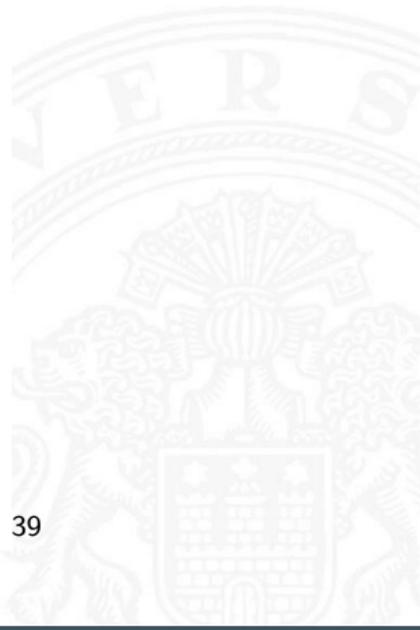
(b)  $f = Mg \cos \theta - Mr \dot{\theta}^2$  : Fall down with constant leg length



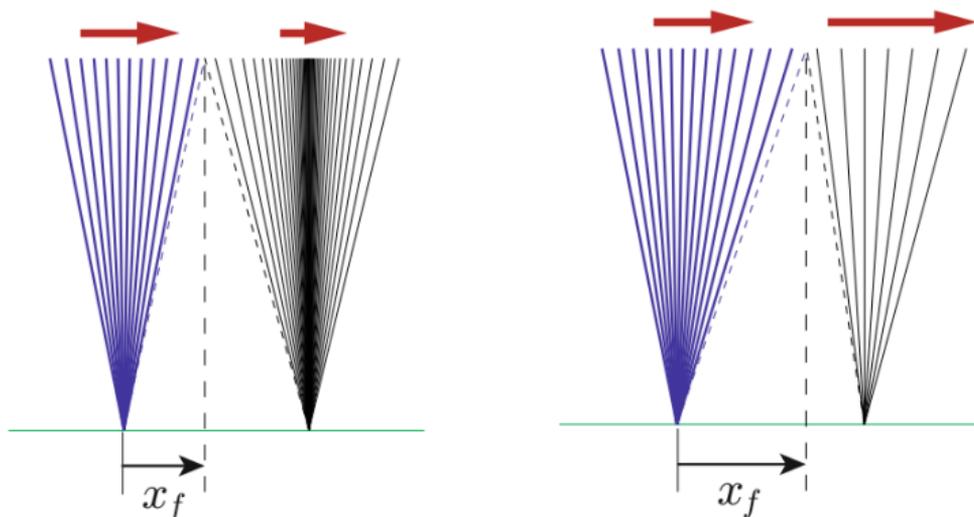
(c)  $f = Mg$  : Fall down and acceleration



(d)  $f = Mg / \cos \theta$  : CoM accelerates while keeping the initial height



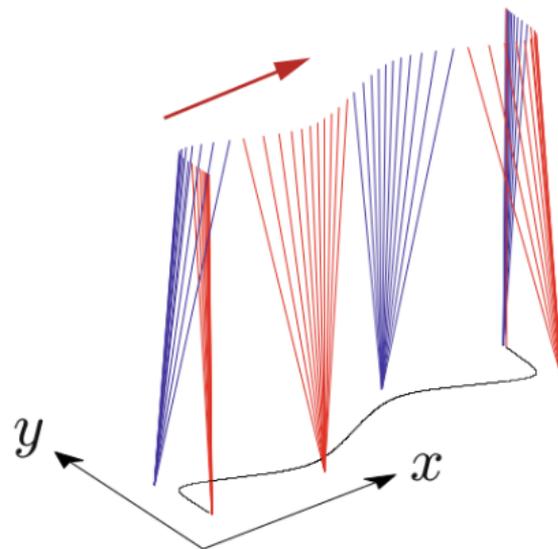
- ▶ Considering fixed step length
- ▶ Earlier touchdown of the next step results slow down
- ▶ Later touchdown of the next step results speed ups



40



- ▶ Transfer to 3D
- ▶ Introduction of lateral movement

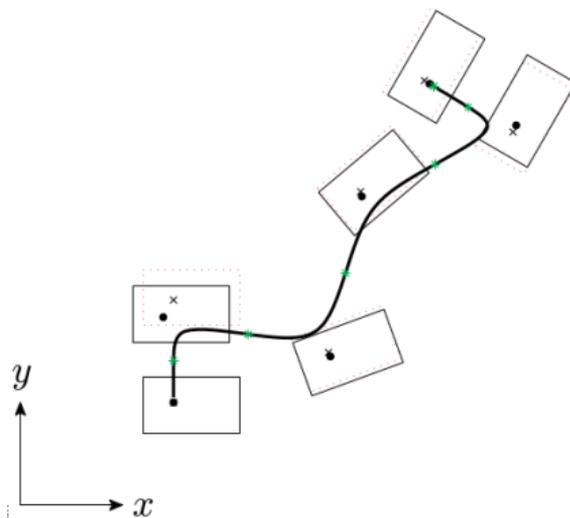


41



# Omni-directional (holonomic) Walking

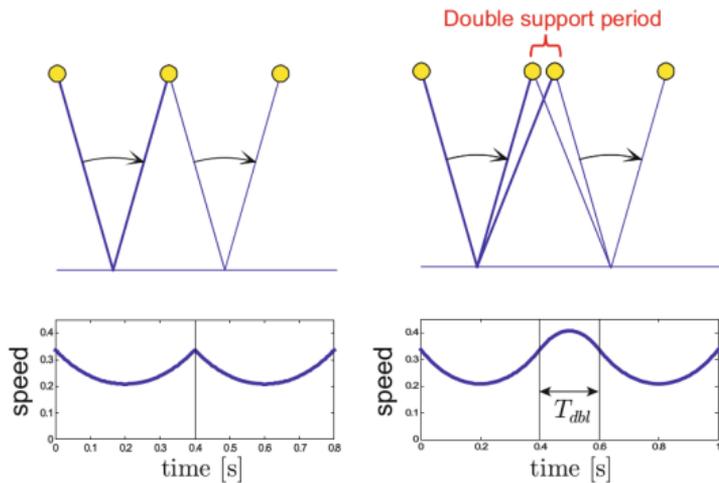
- ▶ Forward ( $x$ )
- ▶ Sideward ( $y$ )
- ▶ Turn (yaw)



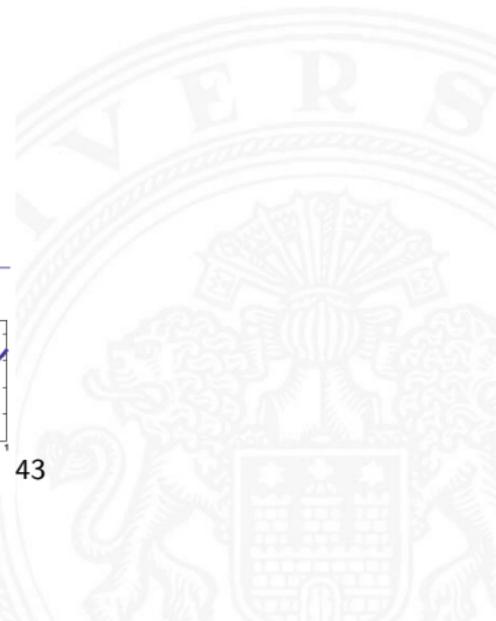
42



- ▶ Accelerations are extreme on support change
- ▶ Not feasible in reality
- ▶ Introduction of a double support phase

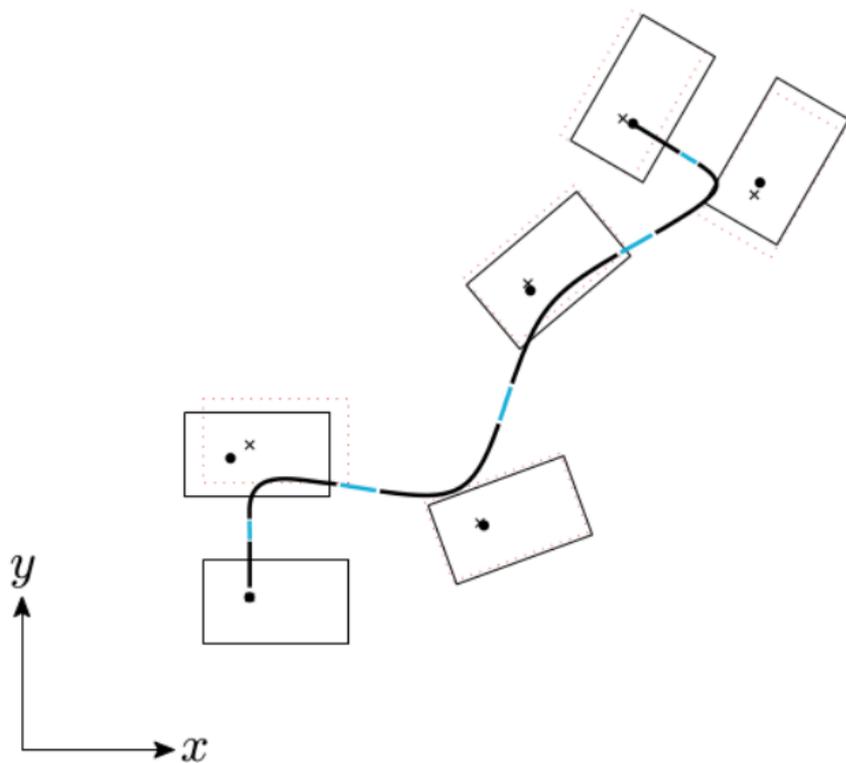


43





# Double Support





45

---

<sup>45</sup> <https://thumbs.dreamstime.com/z/running-robot-27653003.jpg>



- ▶ Why are we not finished yet?



Video





Which senses do you think humans use for walking?





- ▶ Sensors
  - ▶ IMU(s)
  - ▶ Force sensors on foot sole
  - ▶ 6 axis force/torque sensor in ankle
  - ▶ Joint Torques
  - ▶ Camera
- ▶ Model
  - ▶ Joint positions
  - ▶ Link masses and inertia
  - ▶ Rigidity of links (especially foot soles)





- ▶ Simple stopping
- ▶ Counter movements with the arms/torso
- ▶ Change of step position (capture steps)

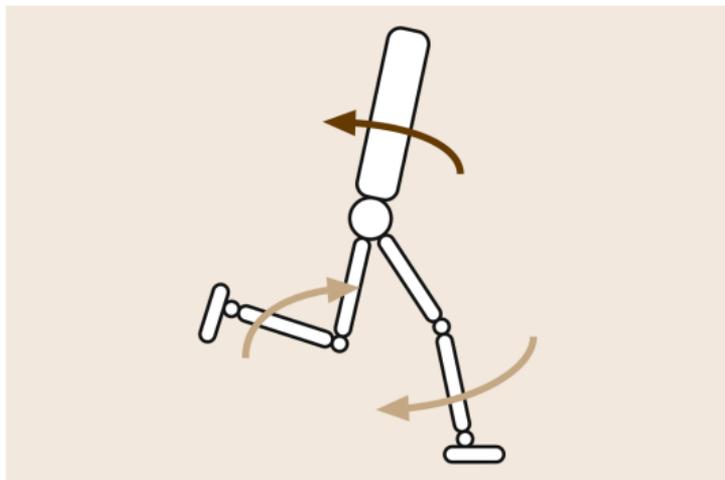


Video



# Counter Movements with Upper Body

- ▶ Rotation around edge of support polygon
- ▶ Introduce counter force with arms/torso or flying leg
- ▶ Flying leg is mostly not usable



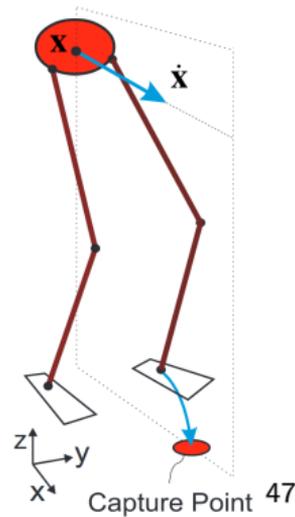
46

Video





- ▶ Capture point is where the robot comes to a complete stop
- ▶ Multiple capture steps may be necessary



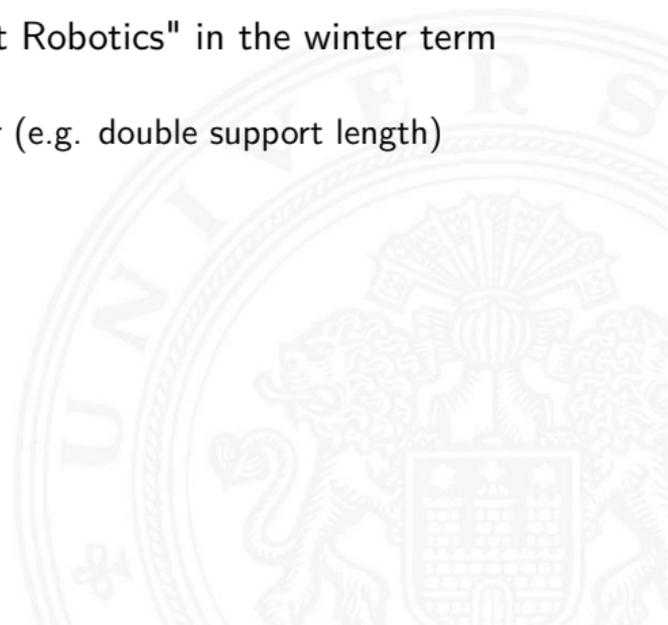
<sup>47</sup> <https://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=6094435>

Video





- ▶ We will not cover machine learning
- ▶ If you are interested join my lecture in "Intelligent Robotics" in the winter term
- ▶ General approaches are:
  - ▶ Learning parameter of a walking pattern generator (e.g. double support length)
  - ▶ Learning neural networks from scratch
  - ▶ Learning from demonstration
  - ▶ Artificial central pattern generators



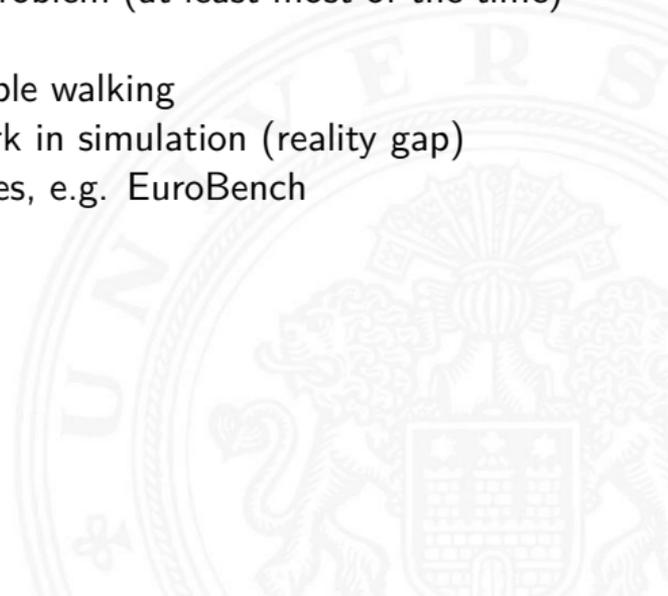


Videos





- ▶ Some very expensive robot manage to solve the problem (at least most of the time) using control theory
- ▶ Cheaper robots still struggle to achieve really stable walking
- ▶ Machine learning approaches still mostly only work in simulation (reality gap)
- ▶ Working on better comparison between approaches, e.g. EuroBench





BALANCE



## System Abilities\*

## Motor skills\*

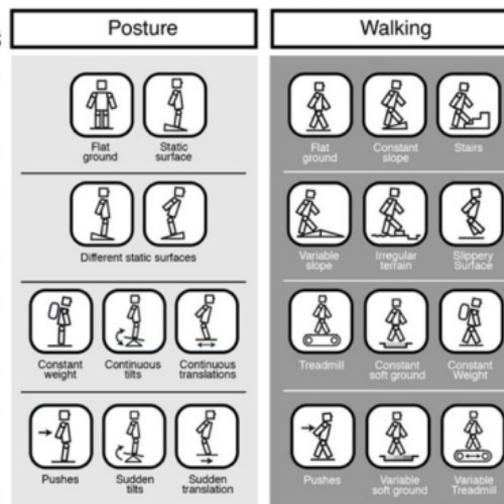
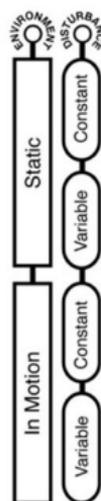
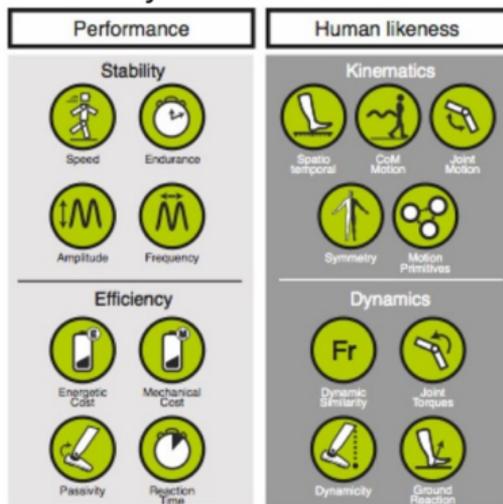
HUMANOIDS



WEARABLE ROBOTS



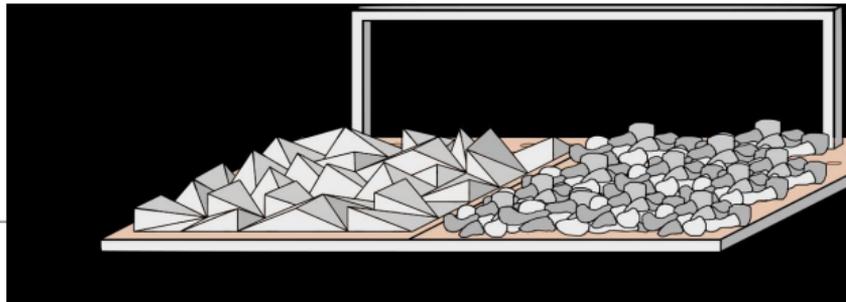
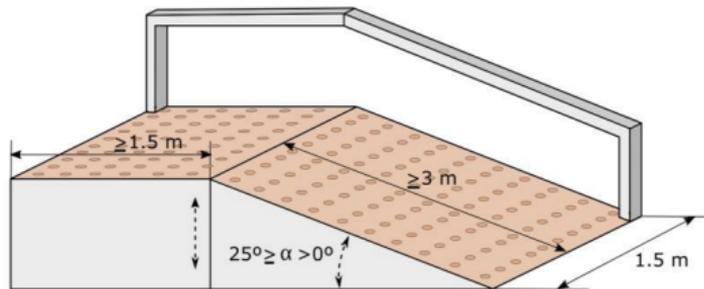
CLINICAL ASSESSMENT



[www.benchmarkinglocomotion.org](http://www.benchmarkinglocomotion.org)

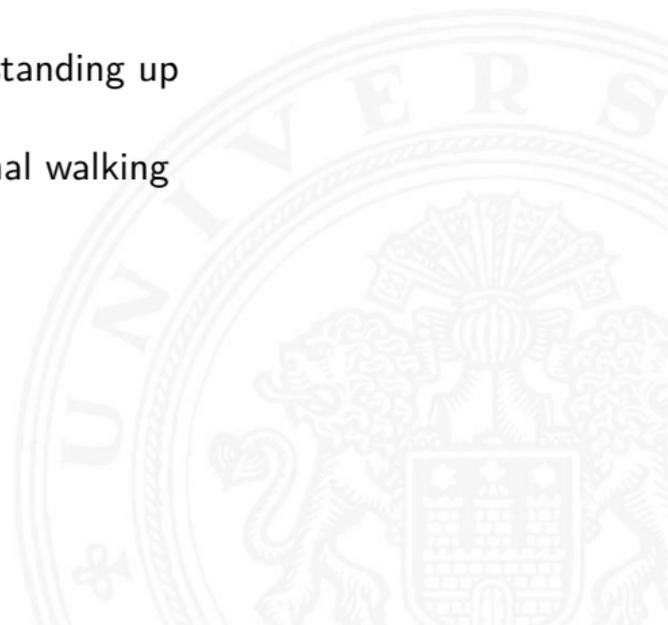
\* Torricelli et al. 2015, Benchmarking Bipedal Locomotion: A Unified Scheme for Humanoids, Wearable Robots, and Humans

48



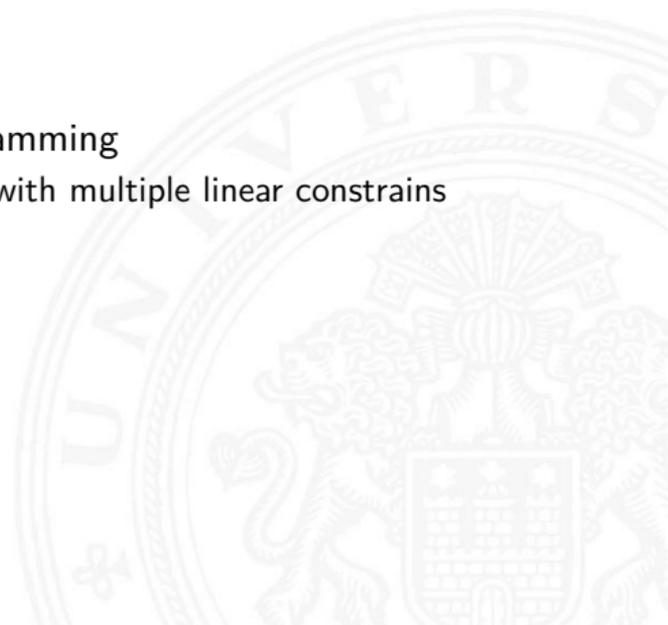


- ▶ Small overview of full body motions
- ▶ Examples are: walking with hand on handrail or standing up
- ▶ Higher complexity since all limbs are involved
- ▶ Breaks assumptions that are often made for normal walking
- ▶ Motions can be periodic or non periodic





- ▶ Using handrail, pushing cart, opening door, holding hands, using walking stick, collaborative carrying
- ▶ Introduces additional forces on the robot
- ▶ Support polygon maybe totally different
- ▶ More complex models have to be used
- ▶ Currently mostly used approach: quadratic programming
  - ▶ Solve problem of optimizing a quadratic function with multiple linear constrains
  - ▶ Use rigid body dynamics together with a model
  - ▶ Problems
    - ▶ Model is not perfect
    - ▶ If caring an object, you need a model of it
    - ▶ Robot is maybe not perfectly rigid





- ▶ Simpler due to known start and end
- ▶ Examples
  - ▶ Standing up
  - ▶ Kicking
  - ▶ Grasping
  - ▶ Waving





- ▶ Keypoint teach in
  - ▶ Put robot into key positions manually
  - ▶ Save joint positions at these points
  - ▶ Interpolate
  - ▶ Useful for simple motions (e.g. waving) or static robots
- ▶ Learning from demonstration
  - ▶ Either demonstrate on the robot itself or by using motion capture
  - ▶ Normally more than one demonstration
  - ▶ Not just simply replaying
- ▶ Cartesian splines
  - ▶ Define trajectories of the limbs with Cartesian splines manually
  - ▶ Comparably easy to do for humans (much better than joint space)
  - ▶ Use inverse kinematics to compute joint goals
  - ▶ Splines configurable with few parameters
  - ▶ Optimize parameters, e.g. using tree-structured parzen estimator



- ▶ DeepLearning
  - ▶ Just let it learn in simulation till it works
  - ▶ Put it on the robot and hope for the best
  - ▶ Reality gap
- ▶ Control Theory
  - ▶ Have an open loop trajectory, e.g. from teach in or LIPM
  - ▶ Use a stability criterion, e.g. ZMP
  - ▶ Adjust joint goals with controller, e.g. PID
- ▶ More on the learning aspect in the intelligent robotics lecture





Questions?





- [1] G.-Z. Yang, R. J. Full, N. Jacobstein, P. Fischer, J. Bellingham, H. Choset, H. Christensen, P. Dario, B. J. Nelson, and R. Taylor, “Ten robotics technologies of the year,” 2019.
- [2] J. K. Yim, E. K. Wang, and R. S. Fearing, “Drift-free roll and pitch estimation for high-acceleration hopping,” in *2019 International Conference on Robotics and Automation (ICRA)*, pp. 8986–8992, IEEE, 2019.
- [3] J. F. Engelberger, *Robotics in service*. MIT Press, 1989.
- [4] K. Fu, R. González, and C. Lee, *Robotics: Control, Sensing, Vision, and Intelligence*. McGraw-Hill series in CAD/CAM robotics and computer vision, McGraw-Hill, 1987.
- [5] R. Paul, *Robot Manipulators: Mathematics, Programming, and Control: the Computer Control of Robot Manipulators*. Artificial Intelligence Series, MIT Press, 1981.
- [6] J. Craig, *Introduction to Robotics: Pearson New International Edition: Mechanics and Control*. Always learning, Pearson Education, Limited, 2013.



- [7] T. Flash and N. Hogan, "The coordination of arm movements: an experimentally confirmed mathematical model," *Journal of neuroscience*, vol. 5, no. 7, pp. 1688–1703, 1985.
- [8] T. Kröger and F. M. Wahl, "Online trajectory generation: Basic concepts for instantaneous reactions to unforeseen events," *IEEE Transactions on Robotics*, vol. 26, no. 1, pp. 94–111, 2009.
- [9] W. Böhm, G. Farin, and J. Kahmann, "A Survey of Curve and Surface Methods in CAGD," *Comput. Aided Geom. Des.*, vol. 1, pp. 1–60, July 1984.
- [10] J. Zhang and A. Knoll, "Constructing Fuzzy Controllers with B-spline Models - Principles and Applications," *International Journal of Intelligent Systems*, vol. 13, no. 2-3, pp. 257–285, 1998.
- [11] M. Eck and H. Hoppe, "Automatic Reconstruction of B-spline Surfaces of Arbitrary Topological Type," in *Proceedings of the 23rd Annual Conference on Computer Graphics and Interactive Techniques, SIGGRAPH '96*, (New York, NY, USA), pp. 325–334, ACM, 1996.



- [12] A. Cowley, W. Marshall, B. Cohen, and C. J. Taylor, “Depth space collision detection for motion planning,” 2013.
- [13] Hornung, Armin and Wurm, Kai M. and Bennewitz, Maren and Stachniss, Cyrill and Burgard, Wolfram, “OctoMap: an efficient probabilistic 3D mapping framework based on octrees,” *Autonomous Robots*, vol. 34, pp. 189–206, 2013.
- [14] D. Berenson, S. S. Srinivasa, D. Ferguson, and J. J. Kuffner, “Manipulation planning on constraint manifolds,” in *2009 IEEE International Conference on Robotics and Automation*, pp. 625–632, 2009.
- [15] S. Karaman and E. Frazzoli, “Sampling-based algorithms for optimal motion planning,” *The International Journal of Robotics Research*, vol. 30, no. 7, pp. 846–894, 2011.
- [16] O. Khatib, “The Potential Field Approach and Operational Space Formulation in Robot Control,” in *Adaptive and Learning Systems*, pp. 367–377, Springer, 1986.
- [17] L. E. Kavraki, P. Svestka, J. Latombe, and M. H. Overmars, “Probabilistic roadmaps for path planning in high-dimensional configuration spaces,” *IEEE Transactions on Robotics and Automation*, vol. 12, no. 4, pp. 566–580, 1996.



- [18] J. Kuffner and S. LaValle, “RRT-Connect: An Efficient Approach to Single-Query Path Planning.,” vol. 2, pp. 995–1001, 01 2000.
- [19] J. Starek, J. Gómez, E. Schmerling, L. Janson, L. Moreno, and M. Pavone, “An asymptotically-optimal sampling-based algorithm for bi-directional motion planning,” *Proceedings of the ... IEEE/RSJ International Conference on Intelligent Robots and Systems. IEEE/RSJ International Conference on Intelligent Robots and Systems*, vol. 2015, 07 2015.
- [20] D. Hsu, J. . Latombe, and R. Motwani, “Path planning in expansive configuration spaces,” in *Proceedings of International Conference on Robotics and Automation*, vol. 3, pp. 2719–2726 vol.3, 1997.
- [21] A. H. Qureshi, A. Simeonov, M. J. Bency, and M. C. Yip, “Motion planning networks,” in *2019 International Conference on Robotics and Automation (ICRA)*, pp. 2118–2124, IEEE, 2019.
- [22] J. Schulman, J. Ho, A. Lee, I. Awwal, H. Bradlow, and P. Abbeel, “Finding locally optimal, collision-free trajectories with sequential convex optimization,” in *in Proc. Robotics: Science and Systems*, 2013.



- [23] A. T. Miller and P. K. Allen, “Graspit! a versatile simulator for robotic grasping,” *IEEE Robotics Automation Magazine*, vol. 11, no. 4, pp. 110–122, 2004.
- [24] A. ten Pas, M. Gualtieri, K. Saenko, and R. Platt, “Grasp pose detection in point clouds,” *The International Journal of Robotics Research*, vol. 36, no. 13-14, pp. 1455–1473, 2017.
- [25] L. P. Kaelbling and T. Lozano-Pérez, “Hierarchical task and motion planning in the now,” in *2011 IEEE International Conference on Robotics and Automation*, pp. 1470–1477, 2011.
- [26] N. T. Dantam, Z. K. Kingston, S. Chaudhuri, and L. E. Kavraki, “Incremental task and motion planning: A constraint-based approach.,” in *Robotics: Science and Systems*, pp. 1–6, 2016.
- [27] J. Ferrer-Mestres, G. Francès, and H. Geffner, “Combined task and motion planning as classical ai planning,” *arXiv preprint arXiv:1706.06927*, 2017.
- [28] M. Görner, R. Haschke, H. Ritter, and J. Zhang, “Movelt! Task Constructor for Task-Level Motion Planning,” in *IEEE International Conference on Robotics and Automation (ICRA)*, 2019.



- [29] K. Hauser and J.-C. Latombe, "Multi-modal motion planning in non-expansive spaces," *The International Journal of Robotics Research*, vol. 29, no. 7, pp. 897–915, 2010.
- [30] B. Siciliano and O. Khatib, *Springer handbook of robotics*. Springer, 2016.
- [31] P. Sermanet, C. Lynch, Y. Chebotar, J. Hsu, E. Jang, S. Schaal, S. Levine, and G. Brain, "Time-contrastive networks: Self-supervised learning from video," in *2018 IEEE International Conference on Robotics and Automation (ICRA)*, pp. 1134–1141, IEEE, 2018.
- [32] C. Finn, P. Abbeel, and S. Levine, "Model-agnostic meta-learning for fast adaptation of deep networks," *arXiv preprint arXiv:1703.03400*, 2017.
- [33] R. Brooks, "A robust layered control system for a mobile robot," *Robotics and Automation, IEEE Journal of*, vol. 2, pp. 14–23, Mar 1986.
- [34] M. J. Mataric, "Interaction and intelligent behavior.," tech. rep., DTIC Document, 1994.



- [35] M. P. Georgeff and A. L. Lansky, "Reactive reasoning and planning.," in *AAAI*, vol. 87, pp. 677–682, 1987.
- [36] J. S. Albus, "The nist real-time control system (rcs): an approach to intelligent systems research," *Journal of Experimental & Theoretical Artificial Intelligence*, vol. 9, no. 2-3, pp. 157–174, 1997.
- [37] T. Fukuda and T. Shibata, "Hierarchical intelligent control for robotic motion by using fuzzy, artificial intelligence, and neural network," in *Neural Networks, 1992. IJCNN., International Joint Conference on*, vol. 1, pp. 269–274 vol.1, Jun 1992.
- [38] L. Einig, *Hierarchical Plan Generation and Selection for Shortest Plans based on Experienced Execution Duration*.  
Master thesis, Universität Hamburg, 2015.
- [39] J. Craig, *Introduction to Robotics: Mechanics & Control. Solutions Manual*.  
Addison-Wesley Pub. Co., 1986.



- [40] H. Siegert and S. Bocionek, *Robotik: Programmierung intelligenter Roboter: Programmierung intelligenter Roboter*. Springer-Lehrbuch, Springer Berlin Heidelberg, 2013.
- [41] R. Schilling, *Fundamentals of robotics: analysis and control*. Prentice Hall, 1990.
- [42] T. Yoshikawa, *Foundations of Robotics: Analysis and Control*. Cambridge, MA, USA: MIT Press, 1990.
- [43] M. Spong, *Robot Dynamics And Control*. Wiley India Pvt. Limited, 2008.

