



Universität Hamburg

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Department of Informatics



# Introduction to Robotics

## Lecture 5

**Shuang Li, Jianwei Zhang**

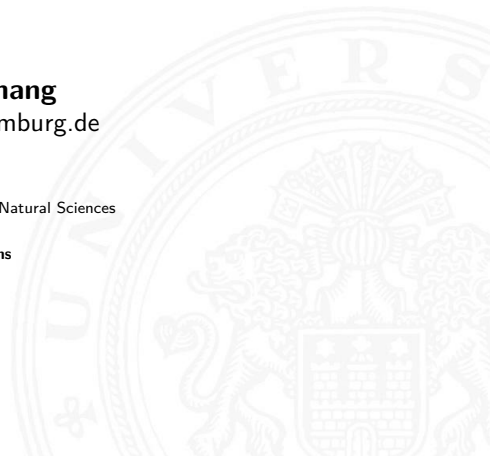
[sli, zhang]@informatik.uni-hamburg.de



University of Hamburg  
Faculty of Mathematics, Informatics and Natural Sciences  
Department of Informatics

**Technical Aspects of Multimodal Systems**

May 6, 2021





Joint velocities  $\Leftrightarrow$  End-effector velocities



## Jacobian

- ▶ Jacobian

$$\delta x_{(m \times 1)} = J_{(m \times n)} \delta q_{(n \times 1)} \quad \text{where} \quad J_{ij}(q) = \frac{\partial}{\partial q_j} f_i(q)$$

- ▶ Angular/Linear velocity Jacobian

$$J = \begin{bmatrix} J_v \\ J_w \end{bmatrix}, \quad \begin{bmatrix} {}^0 v_n \\ {}^0 \omega_n \end{bmatrix} = \begin{bmatrix} J_v \\ J_w \end{bmatrix} \dot{q}$$

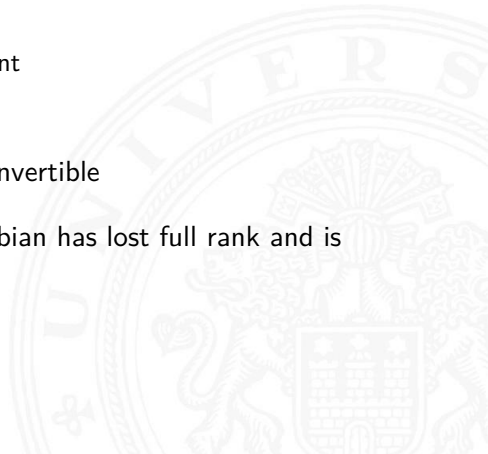
- ▶ Computation of the final Jacobian



- ▶ Geometric singularities:
  - ▶ for any two revolute joints, the joint axes are collinear
  - ▶ any three parallel rotation axes lie in a plane
  - ▶ any four rotational axes intersect at a point
  - ▶ any three coplanar revolute axes intersect at a point
- ▶ Mathematical singularities:

$$\det J = 0 \implies J \text{ is not invertible}$$

Where the determinant is equal to zero, the Jacobian has lost full rank and is singular.





Introduction

Spatial Description and Transformations

Forward Kinematics

Robot Description

Inverse Kinematics for Manipulators

Instantaneous Kinematics

Trajectory Generation 1

- Trajectory and related concepts

- Trajectory generation

- Solutions of trajectory generation

- Optimizing motion

- Application

Trajectory Generation 2

Dynamics

Robot Control





# Outline (cont.)

Trajectory Generation 1

Introduction to Robotics

Path Planning

Task/Manipulation Planning

Telerobotics

Architectures of Sensor-based Intelligent Systems

Summary

Conclusion and Outlook





## Definition

A trajectory is a time history of

position,  
velocity and  
acceleration

for each DOF

Describes motion of TCP frame relative to base frame

- ▶ abstract from joint configuration



- ▶ Changes in position, velocity and acceleration of all joints are analyzed over a period of time
- ▶ Trajectory with  $n$  DOF is a parameterized function  $q(t)$  with values in its motion region.
- ▶ Trajectory  $q(t)$  of a robot with  $n$  DOF is then a vector of  $n$  parameterized functions  $q_i(t)$ ,  $i \in \{1 \dots n\}$  with one common parameter  $t$ :

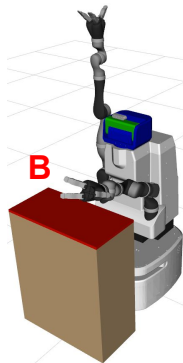
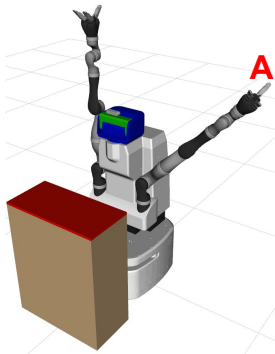
$$q(t) = [q_1(t), q_2(t), \dots, q_n(t)]^T$$



## Problem

The robot is at point A and wants move to point B.

- ▶ How does the robot get to point B?
- ▶ How long does it take the left arm to get to point B?
- ▶ Which possible constraints exist for moving from A to B?







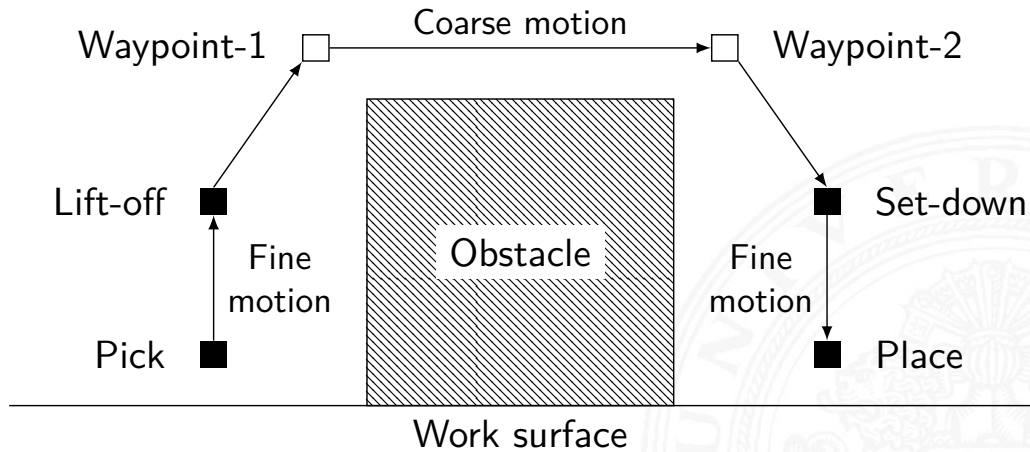
## Problem

The robot is at point A and wants move to point B.

- ▶ How does the robot get to point B?
- ▶ How long does it take the left arm to get to point B?
- ▶ Which possible constraints exist for moving from A to B?

## Solution

- ▶ generate a possible and smooth trajectory
- ▶ describe intermediate poses (waypoints)
  - ▶ usually fixed temporal intervals
- ▶ obey the physical boundaries of the mechanics of the robot





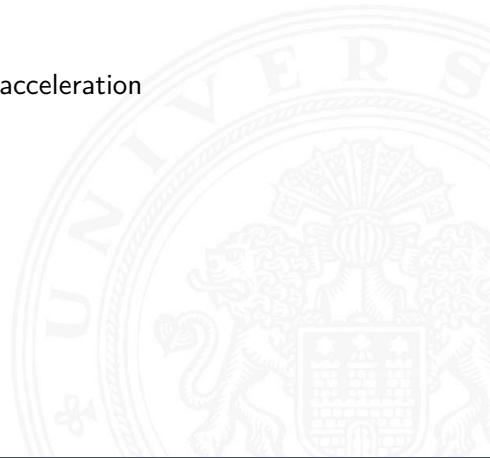
**Pick**  $pos_{Start} = object, vel_{Start} = 0, acc_{Start} = 0$

**Lift-off** limited velocity and acceleration

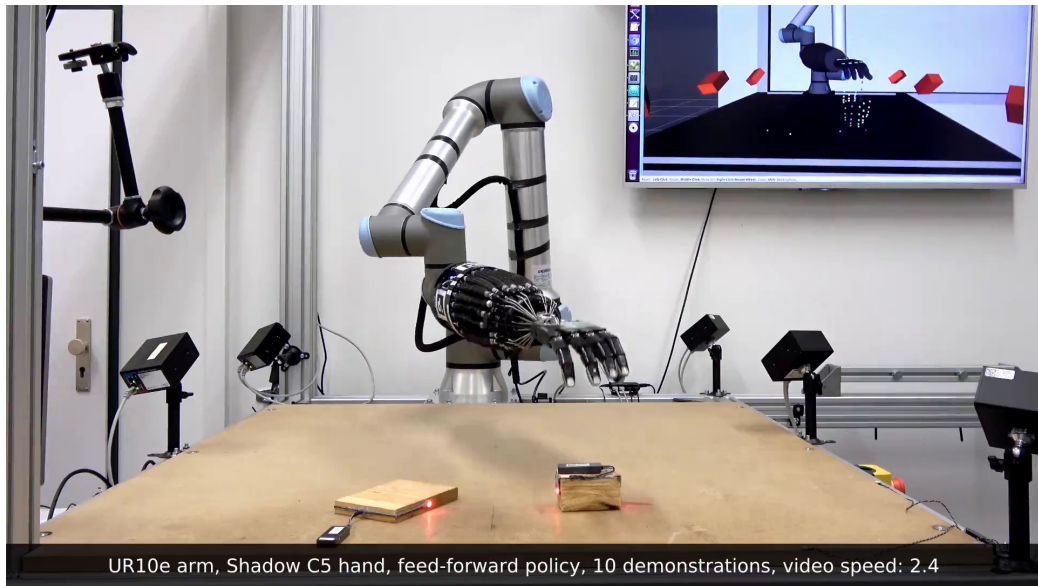
**Motion** continuous via waypoints, full velocity and acceleration

**Set-down** similar to Lift-off

**Place** similar to Pick



# Trajectory planning (cont.)



# Task level planning





## Task

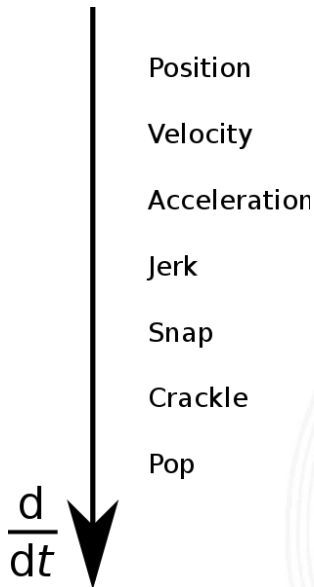
- ▶ find a smooth trajectory for moving the robot from start to goal pose
- ▶ use continuous functions of time



- ▶ A trajectory is  $C^k$ -continuous, if all derivatives up to the  $k$ -th (including) exist and are continuous.
- ▶ A trajectory is called *smooth*, if it is at least  $C^2$ -continuous
  
- ▶  $q(t)$  is the trajectory,
- ▶  $\dot{q}(t)$  is the velocity,
- ▶  $\ddot{q}(t)$  is the acceleration,
- ▶  $\dddot{q}(t)$  is the jerk



# Time-derivatives of position







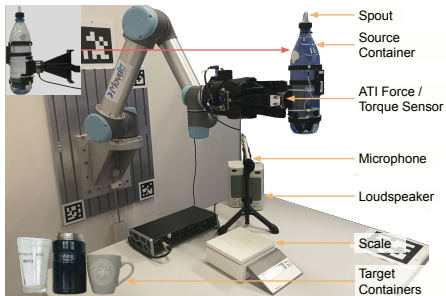
## Task

- ▶ find trajectory for moving the robot from start to goal pose
- ▶ use continuous functions of time

Representation solution:

- ▶ calculation of Cartesian trajectories for the TCP
- ▶ calculation for trajectories in joint space

# Generation of trajectories (cont.)

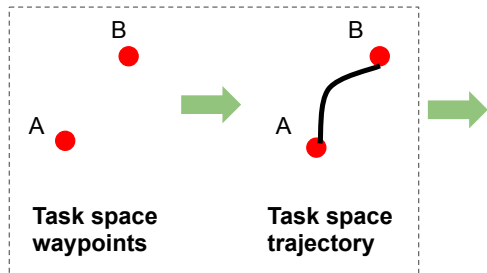


Pouring setup

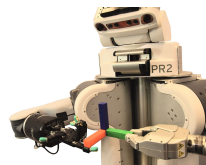


Pushing setup

# Trajectories in Cartesian space



**IK**



**Joint position commands**

Advantages:

- ▶ near to the task specification
- ▶ advantageous for collision avoidance
- ▶ can specify the spatial shape of the path

Disadvantages:

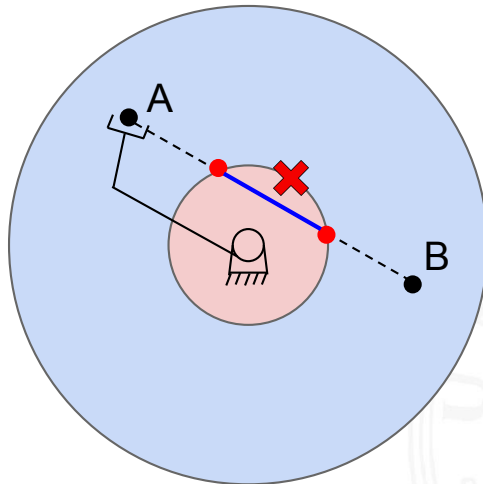
- ▶ more expensive at run time
  - ▶ after the path is calculated need joint angles in a lot of points by IK
- ▶ Discontinuity problems



# Difficulties of trajectories in Cartesian space

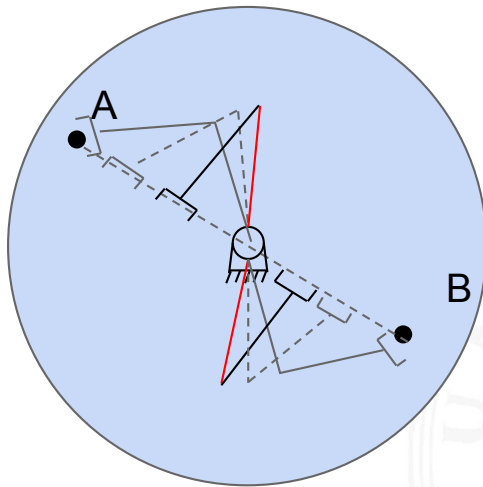
## 1. Waypoints cannot be realized

- ▶ workspace boundaries, object collision, self-collision



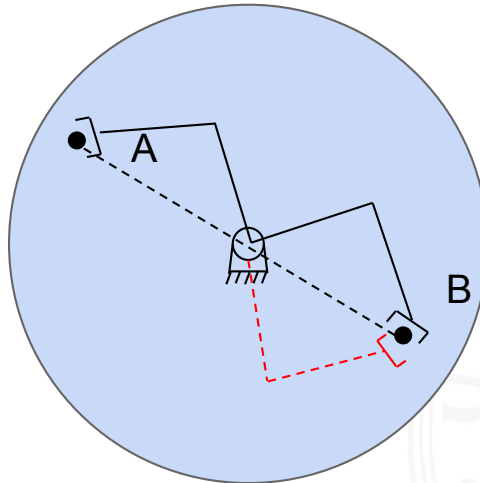


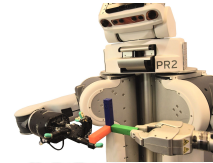
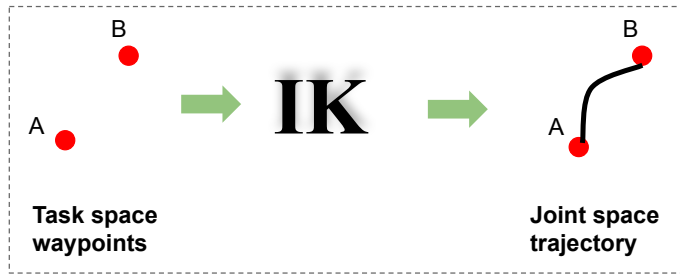
2. Velocities in the vicinity of singular configurations are too high



# Difficulties of trajectories in Cartesian space (cont.)

3. Start and end configurations can be achieved, but there are different solutions
  - ▶ ambiguous solutions





**Joint position commands**

Joint space:

- ▶ no inverse kinematics in joint space required
- ▶ the planned trajectory can be immediately applied
- ▶ no problem with singularities
- ▶ physical joint constraints can be considered



## Naive approach

Set the pose for the next time step (e.g. 10 ms later) to B.

- ▶ possible only in simulation
- ▶ the moving distance for a manipulator at the next time step may be too large (velocity approaches  $\infty$ )



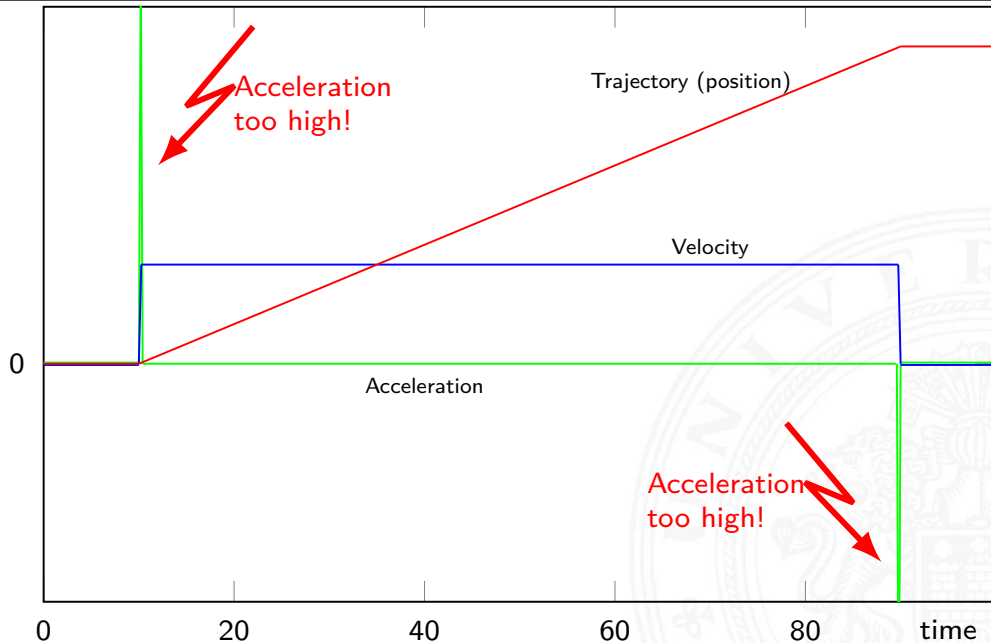


## Next best approach

- ▶ divide distance between A and B to shorter (sub-)distances
- ▶ use linear interpolation for these (sub-)distances
- ▶ respect the maximum velocity constraint



# Linear interpolation – visualization





## Problem

The physical constraints are violated

- ▶ joint velocity is limited by maximum motor rotation speed
- ▶ joint acceleration is limited by maximum motor torque

Implicitly these constraints are valid for motion in cartesian space.

- ▶ robot dynamics (joint moments resulting from the robot motion) affect the boundary condition

## Solution

- ▶ dynamical trajectory generation
- ▶ advanced optimization methods → current topic of research

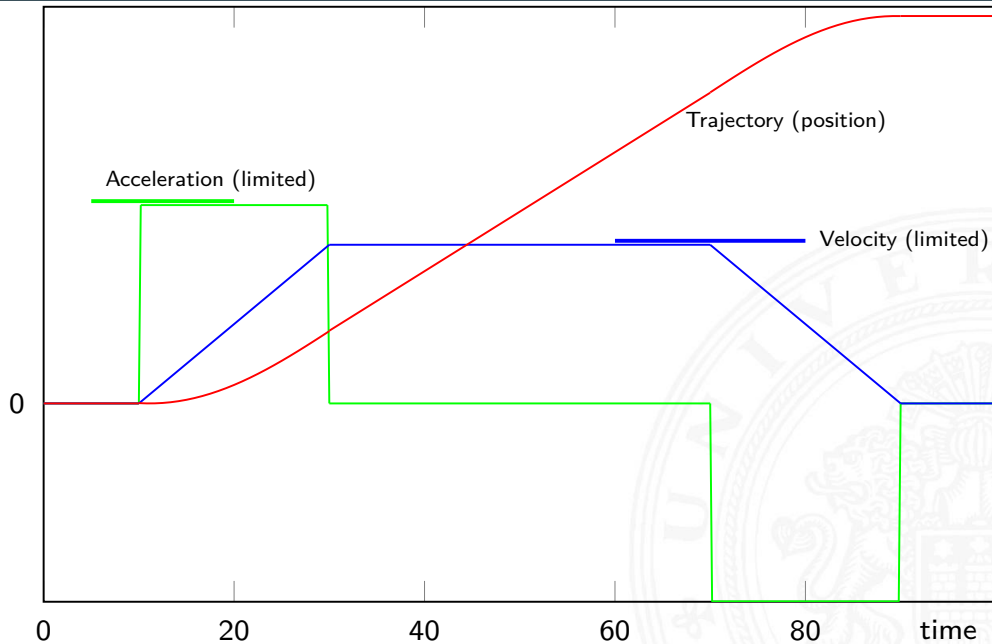


## Next best approach

- ▶ Limitation of joint velocity and acceleration
- ▶ Two different methods
  - ▶ trapezoidal interpolation
  - ▶ polynomial interpolation

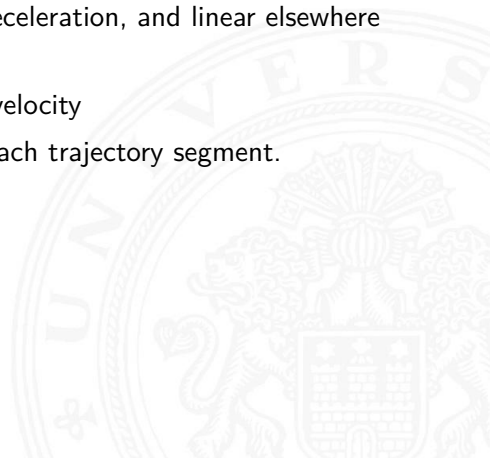


# Trapezoidal interpolation – visualization



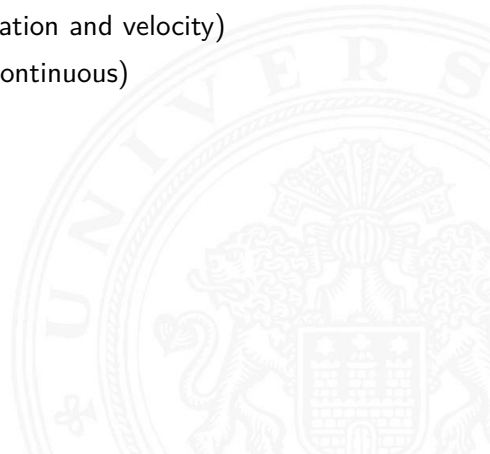


- ▶ Position is quadratic during acceleration and deceleration, and linear elsewhere
  - ▶ Linear segment with Parabolic Blends
- ▶ Velocity linearly ramps up/down to maximum velocity
- ▶ Acceleration and deceleration is constant for each trajectory segment.





- ▶ consider joint velocity and acceleration constraints
- ▶ optimal time usage (move with maximum acceleration and velocity)
- ▶ acceleration is not differentiable (the jerk is not continuous)
- ▶ start and end velocity equals 0
  - ▶ not sensible for concatenating trajectories
  - ▶ improved by polynomial interpolation





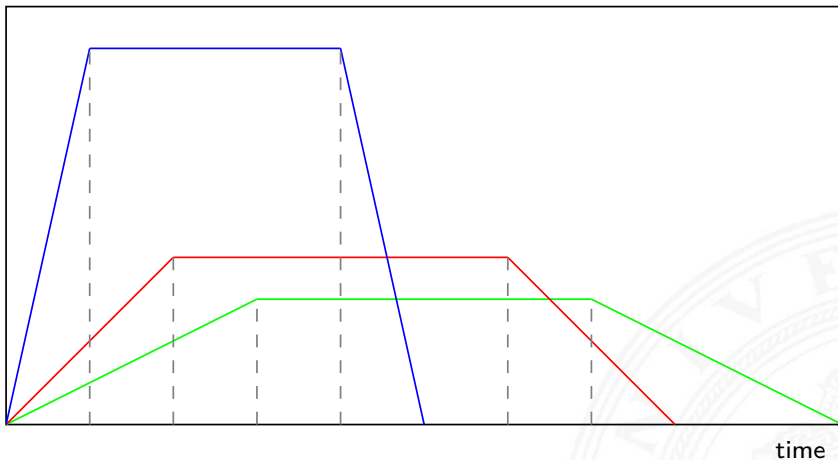
## Problem

### Multidimensional trapezoidal interpolations

- ▶ different run time for joints (or cartesian dimensions)
- ▶ multiple velocity and acceleration constraints
- ▶ results in various time switch points
  - ▶ from acceleration to continuous velocity
  - ▶ from continuous velocity to deceleration
  - ▶ moving along a line in joint/cartesian space is impossible.



# Trapezoidal interpolation – constraints

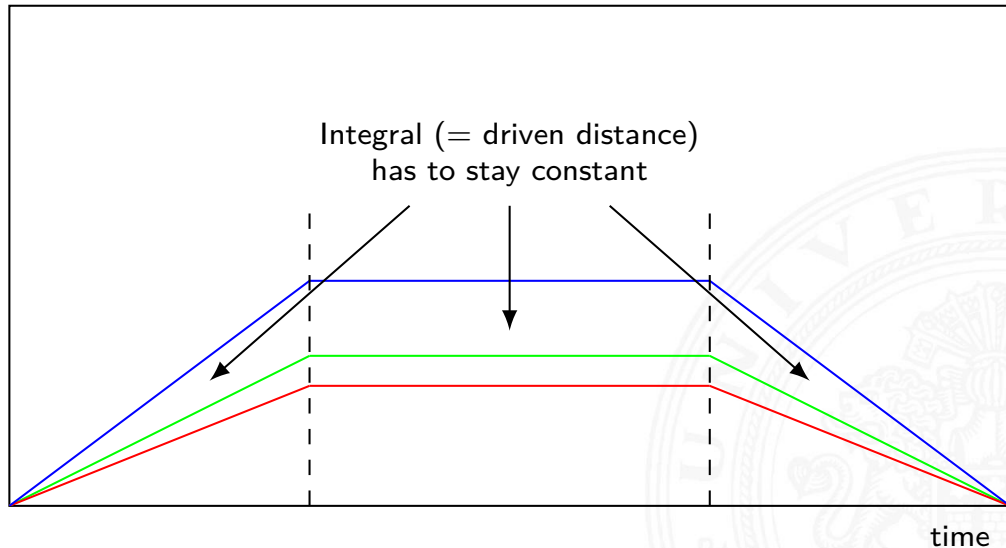


## Solution

- ▶ Normalization to the joint that takes longest to reach its goal
- ▶ Synchronize phase switching points and overall execution time

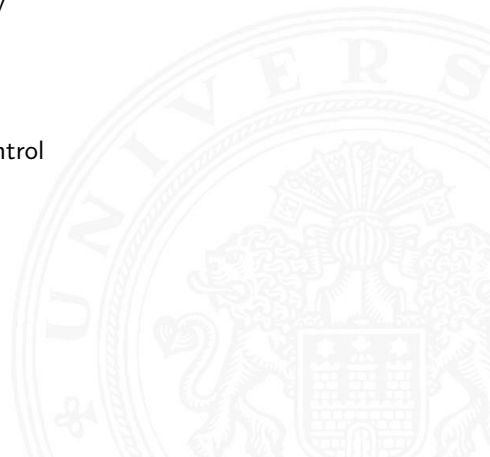


Normalize to the slowest joint



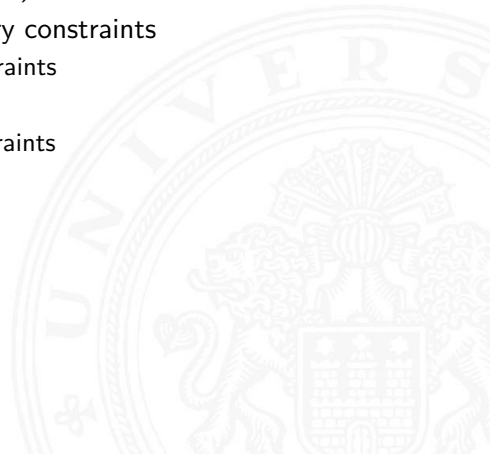


- ▶ Consider velocity and acceleration boundary conditions
  - ▶ calculation of extremum and duration of trajectory
- ▶ Acceleration differentiable
  - ▶ continuous jerk
  - ▶ smooth trajectory
  - ▶ interesting only in the theory – for momentum control
- ▶ Start and end velocity may be  $\neq 0$ 
  - ▶ sensible for concatenating trajectories

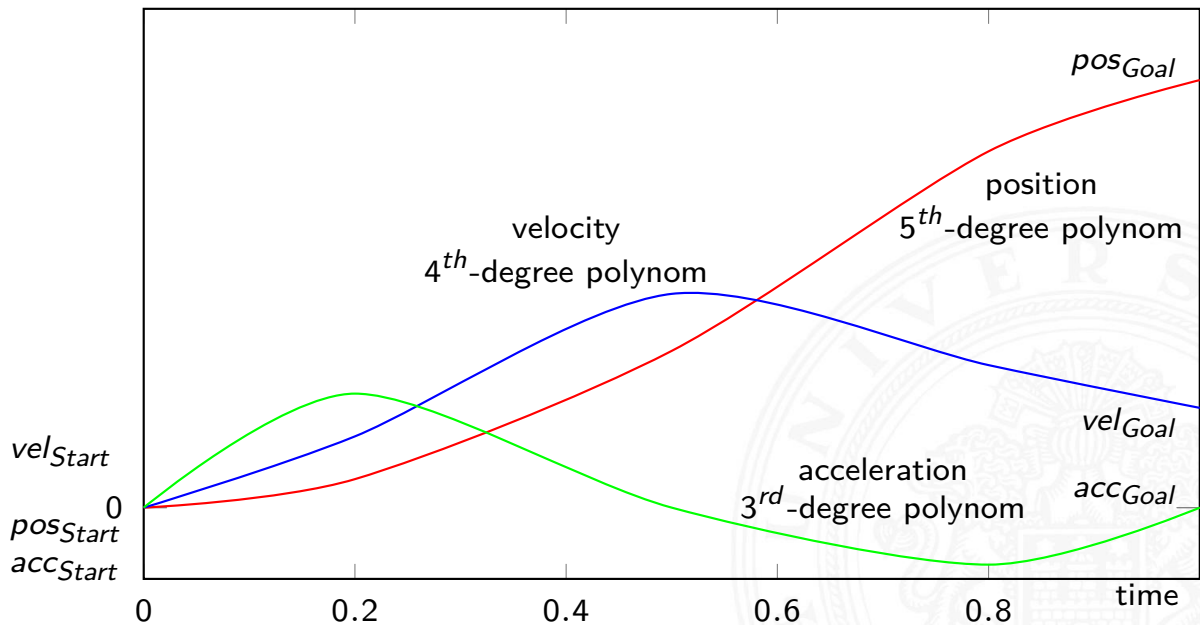




- ▶ Usually a polynomial with degree of 3 (cubic spline) or 5
- ▶ Calculation of coefficient with respect to boundary constraints
  - ▶  $3^{rd}$ -degree polynomial: consider 4 boundary constraints
    - ▶ position and velocity; start and goal
  - ▶  $5^{th}$ -degree polynomial: consider 6 boundary constraints
    - ▶ position, velocity and acceleration; start and goal



# Polynomial interpolation (cont.)





- ▶ third-degree polynomial  $\Rightarrow$  four constraints(position and velocity; start and goal):

$$\theta(t) = a_0 + a_1t + a_2t^2 + a_3t^3$$

$$\dot{\theta}(t) = a_1 + 2a_2t + 3a_3t^2$$

$$\ddot{\theta}(t) = 2a_2 + 6a_3t$$

- ▶ if the start and end velocity is 0 then

$$\theta(0) = \theta_0 \tag{36}$$

$$\theta(t_f) = \theta_f \tag{37}$$

$$\dot{\theta}(0) = 0 \tag{38}$$

$$\dot{\theta}(t_f) = 0 \tag{39}$$



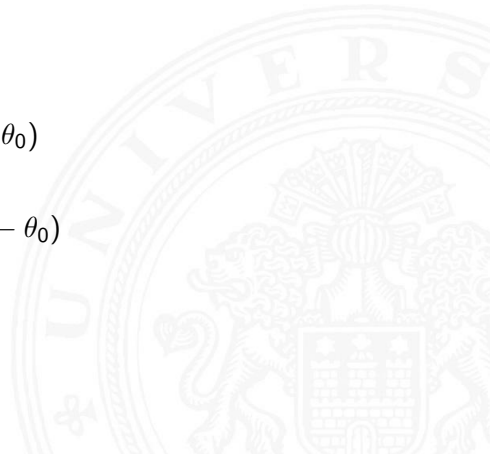
► The solution

$$\text{eq. (36)} \quad a_0 = \theta_0$$

$$\text{eq. (38)} \quad a_1 = 0$$

$$a_2 = \frac{3}{t_f^2}(\theta_f - \theta_0)$$

$$a_3 = -\frac{2}{t_f^3}(\theta_f - \theta_0)$$





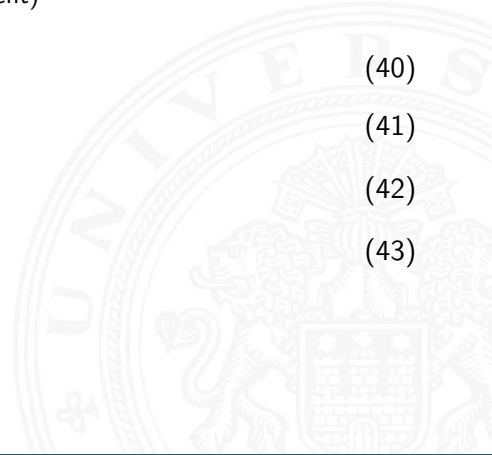
- ▶ Similar to the previous example:
  - ▶ positions of waypoints are given (same)
  - ▶ velocities of waypoints are different from 0 (different)

$$\theta(0) = \theta_0 \quad (40)$$

$$\theta(t_f) = \theta_f \quad (41)$$

$$\dot{\theta}(0) = \dot{\theta}_0 \quad (42)$$

$$\dot{\theta}(t_f) = \dot{\theta}_f \quad (43)$$







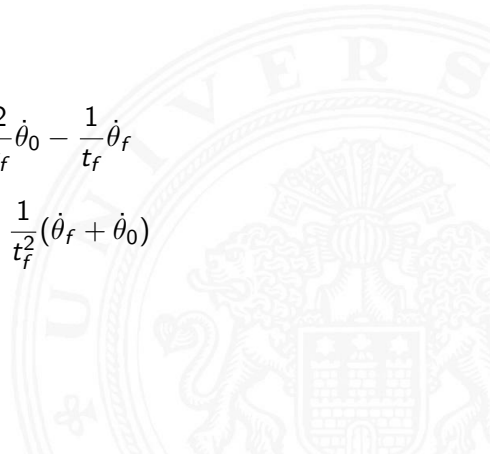
► The solution

$$\text{eq. (40)} \quad a_0 = \theta_0$$

$$\text{eq. (42)} \quad a_1 = \dot{\theta}_0$$

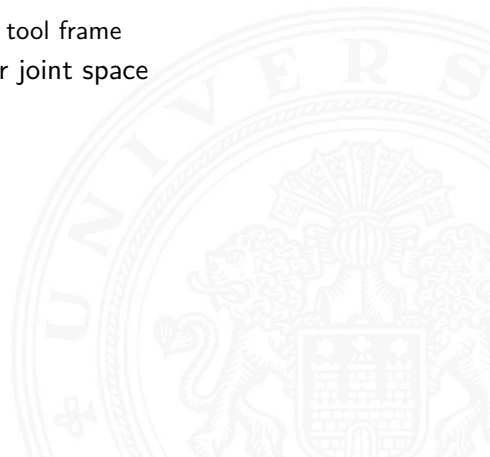
$$a_2 = \frac{3}{t_f^2}(\theta_f - \theta_0) - \frac{2}{t_f}\dot{\theta}_0 - \frac{1}{t_f}\dot{\theta}_f$$

$$a_3 = -\frac{2}{t_f^3}(\theta_f - \theta_0) + \frac{1}{t_f^2}(\dot{\theta}_f + \dot{\theta}_0)$$





- ▶ Manually specify waypoints
  - ▶ based on cartesian linear and angle velocity of the tool frame
- ▶ Automatic calculation of waypoints in cartesian or joint space
  - ▶ based on heuristics
- ▶ Automatic determination of the parameters
  - ▶ based on continuous acceleration at the waypoints



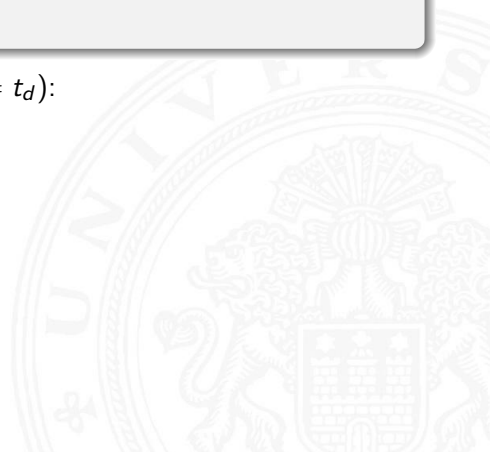


## Example 5<sup>th</sup>-degree

$$\theta(x) = a_0 + a_1 t + a_2 t^2 + a_3 t^3 + a_4 t^4 + a_5 t^5$$

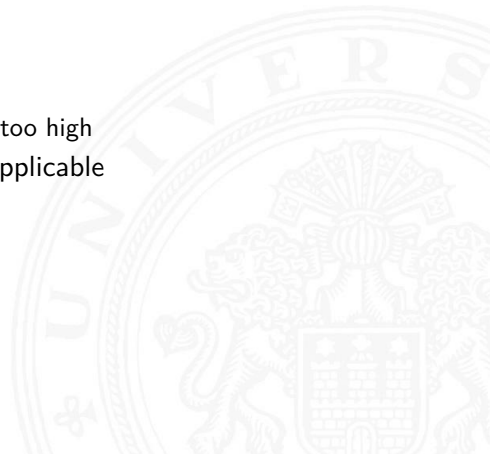
Boundary conditions for start ( $x = t_0$ ) and goal ( $x = t_d$ ):

- ▶  $\theta(t_0) = pos_{Start}, \theta(t_d) = pos_{Goal}$
- ▶  $\dot{\theta}(t_0) = vel_{Start}, \dot{\theta}(t_d) = vel_{Goal}$
- ▶  $\ddot{\theta}(t_0) = acc_{Start}, \ddot{\theta}(t_d) = acc_{Goal}$





- ▶ The smoothest curves are generated by infinitely often differentiable functions.
  - ▶  $e^x$
  - ▶  $\sin(x)$ ,  $\cos(x)$
  - ▶  $\log(x)$  (for  $x > 0$ )
  - ▶ ...
- ▶ Polynomials are suitable for interpolation
  - ▶ Problem: oscillations caused by a degree which is too high
- ▶ Piecewise polynomials with specified degree are applicable
  - ▶ cubic polynomial
  - ▶ splines
  - ▶ B-Splines
  - ▶ ...





If the curve in the  $n$ -dimensional space is given by

$$\mathbf{q}(t) = [q^1(t), q^2(t), \dots, q^n(t)]^T$$

then the **arc length** can be defined as follows:

$$s = \int_0^t \|\dot{\mathbf{q}}(t)\|_2 dt$$

where  $\|\dot{\mathbf{q}}(t)\|_2$  is the euclidean norm of vector  $d\mathbf{q}(t)/dt$  and is labeled as a flow velocity along the curve.

$$\|\mathbf{x}\|_2 := \sqrt{x_1^2 + \dots + x_n^2}$$



With the following two points given

$$\mathbf{p}_0 = \mathbf{q}(t_s) \text{ und } \mathbf{p}_1 = \mathbf{q}(t_f),$$

the arc length  $L$  between  $\mathbf{p}_0$  and  $\mathbf{p}_1$  is the integral:

$$L = \int_{\mathbf{p}_0}^{\mathbf{p}_1} ds = \int_{t_s}^{t_f} \|\dot{\mathbf{q}}(t)\|_2 dt$$

*“The trajectory parameters should be calculated in the way that the arc length  $L$  under the given constraints has the shortest possible value.”*

## Curvature

Defines the sharpness of a curve. A straight line has zero curvature. Curvature of large circles is smaller than of small circles.

At first the *unit vector* of a curve  $\mathbf{q}(t)$  can be defined as

$$\mathbf{U} = \frac{d\mathbf{q}(t)}{ds} = \frac{d\mathbf{q}(t)/dt}{ds/dt} = \frac{\dot{\mathbf{q}}(t)}{|\dot{\mathbf{q}}(t)|}$$

If  $s$  is the parameter of the *arc length* and  $\mathbf{U}$  as the *unit vector* is given, the **curvature** of curve  $\mathbf{q}(t)$  can be defined as

$$\kappa(s) = \left| \frac{d\mathbf{U}}{ds} \right|$$



The **bending energy** of a smooth curve  $\mathbf{q}(t)$  over the interval  $t \in [0, T]$  is defined as

$$E = \int_0^L \kappa(s)^2 ds = \int_0^T \kappa(t)^2 |\dot{\mathbf{q}}(t)| dt$$

where  $\kappa(t)$  is the curvature of  $\mathbf{q}(t)$ .

*“The bending energy  $E$  of a trajectory should be as small as possible under consideration of the arc length.”*





If a motion consists of  $n$  successive segments

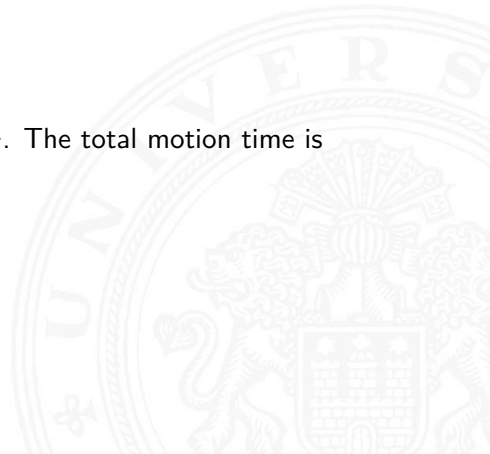
$$q_j, j \in \{1 \dots n\}$$

then

$$u_j = t_{j+1} - t_j$$

is the required time for the motion in the segment  $q_j$ . The total motion time is

$$T = \sum_{j=1}^{n-1} u_j$$





- ▶ Proposed by Flash & Hogan (1985) [7]
- ▶ Optimization Criterion minimizes the jerk in the trajectory

$$H(x(t)) = \frac{1}{2} \int_{t=t_i}^{t_f} \ddot{x}^2 dt$$

- ▶ The minimum-jerk solution can be written as:

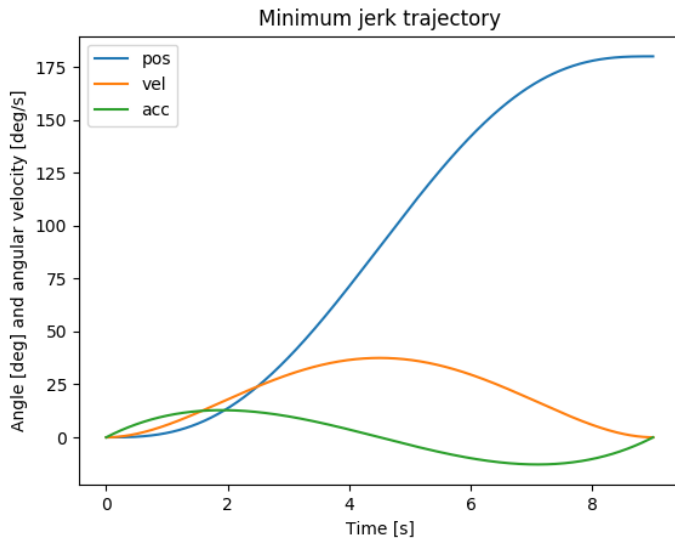
$$x(t) = x_i + (x_i - x_f) \left( 15 \left( \frac{t}{d} \right)^4 - 6 \left( \frac{t}{d} \right)^5 - 10 \left( \frac{t}{d} \right)^3 \right)$$

- ▶ Predicts bell shaped velocity profiles

$$\dot{x}(t) = \frac{1}{d} (x_i - x_f) \left( 60 \left( \frac{t}{d} \right)^3 - 30 \left( \frac{t}{d} \right)^4 - 30 \left( \frac{t}{d} \right)^2 \right)$$



# Minimum jerk trajectory (cont.)





The borders for the minimum motion time  $T_{min}$  for the trajectory  $\mathbf{q}_j^i(t)$  are defined over dynamical parameters of all joints.

For joint  $i \in \{1 \dots n\}$  of trajectory part  $j \in \{1 \dots m\}$  this kind of constraint can be described as follows

$$|\dot{q}_j^i(t)| \leq \dot{q}_{max}^i \quad (44)$$

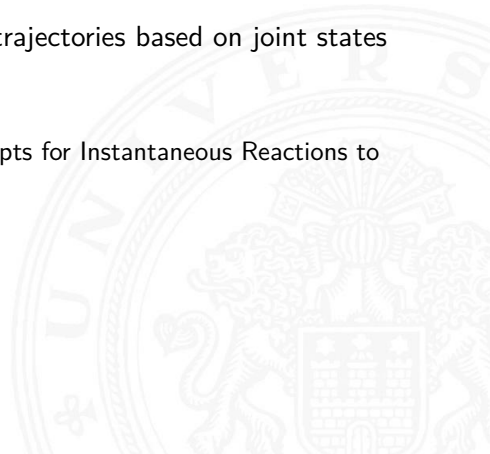
$$|\ddot{q}_j^i(t)| \leq \ddot{q}_{max}^i \quad (45)$$

$$|m_j^i(t)| \leq m_{max}^i \quad (46)$$

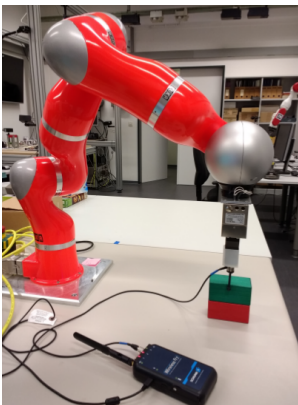
- ▶  $m^i$  is the torque (moment of force) for the joint  $i$  and can be calculated from the dynamical equation (motion equation).
- ▶  $\dot{q}_{max}^i$ ,  $\ddot{q}_{max}^i$  and  $m_{max}^i$  represent the important parameters of the dynamical capacity of the robot.



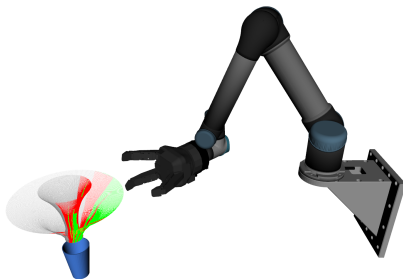
- ▶ Reflexxes Motion Libraries (Download, Overview)
- ▶ specialize on instantaneously generating smooth trajectories based on joint states and their limits
- ▶ Prof. Dr. Torsten Kroeger
  - ▶ paper: Online Trajectory Generation: Basic Concepts for Instantaneous Reactions to Unforeseen Events [8]



- ▶ Real-time object shape detection using ROS, the KUKA LWR4+ and a force/torque Sensor
  - ▶ to specify the target position and target velocity at the target position



- ▶ Adaptive pouring of liquids based on human motions using a Robotic Arm
  - ▶ to recalculate the speeds of a joint trajectory (returned by CCP) to match the original time-line of the



25

<sup>24</sup>[https://tams.informatik.uni-hamburg.de/publications/2017/MSc\\_Stephan\\_Rau.pdf](https://tams.informatik.uni-hamburg.de/publications/2017/MSc_Stephan_Rau.pdf)

<sup>25</sup>[https://tams.informatik.uni-hamburg.de/publications/2018/MSc\\_Jeremias\\_Hartz.pdf](https://tams.informatik.uni-hamburg.de/publications/2018/MSc_Jeremias_Hartz.pdf)



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